

Study of the finite-temperature physics of a lattice SU(4) gauge BSM model.

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Motivation

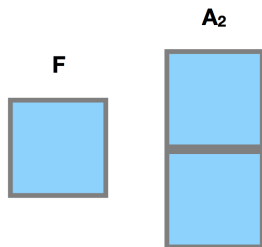
- ▶ Study of $SU(4)$ gauge theory with fermions in multiple representations in $(3+1)D$.
- ▶ Interesting in the context of partial compositeness^{1,2}(W. Jay's talk).
- ▶ Looking for **confinement** and **chiral** transitions.
- ▶ Can have different transitions for each representation.

¹D. B. Kaplan and H. Georgi, Phys. Lett. B 136, 183 (1984).

²G. Ferretti, JHEP 06 (2014), 142.

Model details

- ▶ SU(4) gauge theory.
- ▶ NDS action³(nHYP Dislocation Suppression).
- ▶ Clover improved Wilson fermions.
- ▶ 2 flavors of fermions in the fundamental representation(F).
- ▶ 2 flavors of fermions in two-index anti-symmetric representation (A_2)
- ▶ 3D bare parameter space : $\beta, \kappa_4, \kappa_6$.
- ▶ Finite temperature study.



³DeGrand, Shamir, Svetitsky 2014

Types of transitions (... for this talk)

Confinement transition

- ▶ Low temperatures \rightarrow color singlets. No individual quarks.
- ▶ High temperatures \rightarrow Individual quarks can exist.
- ▶ Transition line moves with N_t .

Bulk Transition

- ▶ Unphysical lattice transition.
- ▶ Transition line at fixed bare parameters is independent of N_t .

Polyakov loop expectation value

In pure gauge theory

- ▶ $\langle P \rangle$ order parameter for SSB of centre symmetry $Z(4)$.
- ▶ Confined $\implies \langle P \rangle = 0$.
- ▶ Deconfined, $\implies \langle P \rangle \neq 0$.

Full multi-rep theory

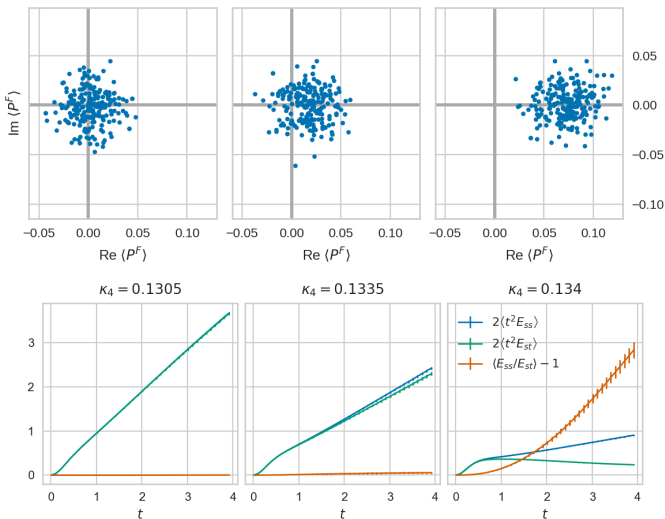
- ▶ F fermions break $Z(4)$ completely.
- ▶ A_2 fermions break $Z(4)$ to $Z(2)$.
- ▶ Pseudo-order parameter.
- ▶ $\langle P \rangle = e^{-\beta F}$
- ▶ $P^F \equiv e^{-\text{Free energy of } F \text{ quark}}$.
- ▶ Similarly, can define $P^{A_2} \equiv e^{-\text{Free energy of } A_2 \text{ quark}}$.
- ▶ Can look at confinement-deconfinement for each representation.

Flow anisotropy

- ▶ Wilson flow observable $\langle t^2 E(t) \rangle$ can be used to diagnose the phase⁴.
- ▶ $\langle t^2 E(t) \rangle = \langle t^2 E_{ss}(t) \rangle + \langle t^2 E_{st}(t) \rangle$
- ▶ Spatial and temporal values deviate in deconfined phase.
- ▶ In previous work, $t^2 \langle E_{ss}(t) - E_{st}(t) \rangle$.
- ▶ We use $\langle \frac{E_{ss}(t)}{E_{st}(t)} \rangle - 1$.

⁴ S. Datta, S. Gupta, and A. Lytle, Phys. Rev. D94, 094502 (2016);

M. Wandelt, F. Knechtli, and M. Gunther, JHEP 10, 061 (2016)

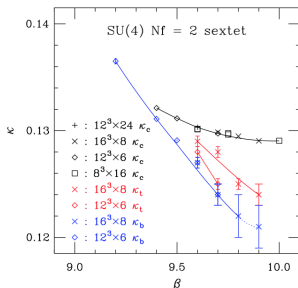


Lattice simulation details

- ▶ Finite temperature study.
- ▶ Lattice sizes $12^3 \times 6$ and $16^3 \times 8$.
- ▶ Both diagnostics (PL and flow) are consistent.
- ▶ Empirically determine a cut to distinguish confined and deconfined phases
- ▶ For Polyakov loop, the variance of $\arg(P) < 1.0$.
- ▶ 30-200 independent configs for each ensemble.
- ▶ Around 500 ensembles.

Sextet-only limit

Previous work⁵ with A_2
fermions (different action)

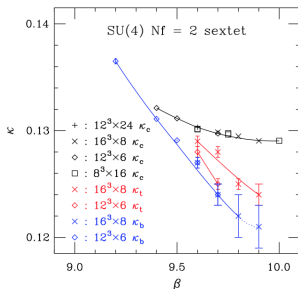


- ▶ Bulk transition followed by
- ▶ Confinement transition
- ▶ $\kappa_{critical}$

⁵T. DeGrand, Y. Liu, E. Neil, Y. Shamir, B. Svetitsky, PRD 91, (2015).

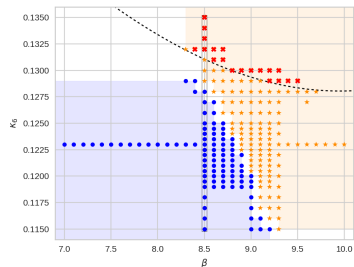
Sextet-only limit

Previous work⁵ with A_2 fermions (different action)



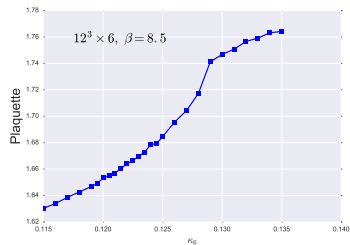
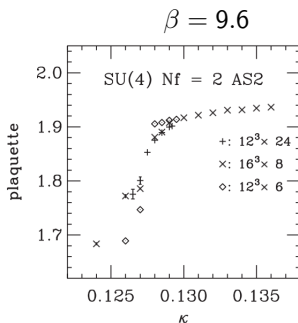
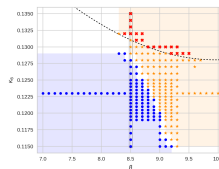
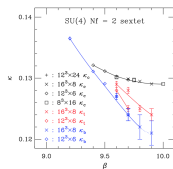
- ▶ Bulk transition followed by
- ▶ Confinement transition
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NDS action in the A_2 -only limit. ($12^3 \times 6$ lattice)



- ▶ Confinement transition
- ▶ $\kappa_{critical}$

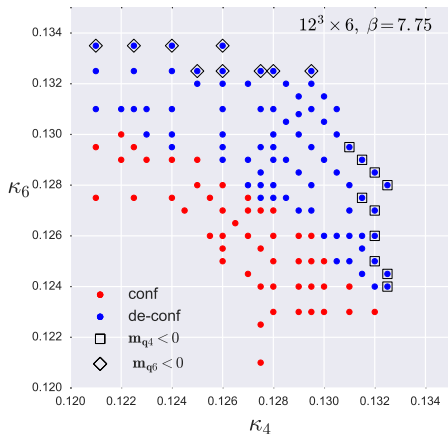
⁵T. DeGrand, Y. Liu, E. Neil, Y. Shamir, B. Svetitsky, PRD 91, (2015).



No Bulk transition in region of interest with NDS action.

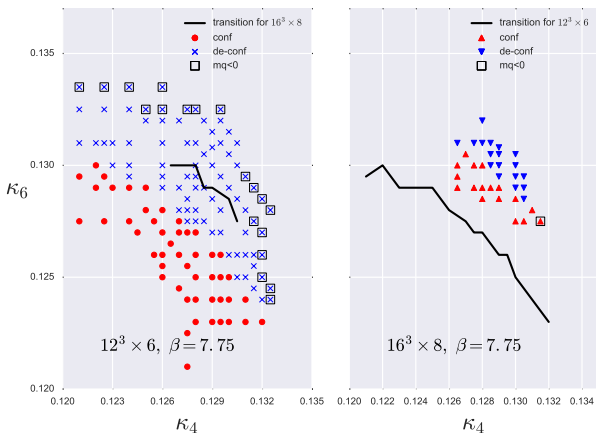
Phase diagram

Simulation with both representations:



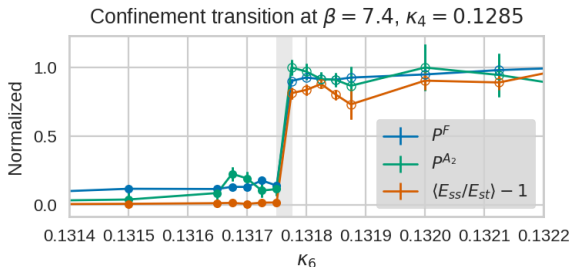
Variation with temperature

- Curve shifts to the right as temperature $T = \frac{1}{aN_t}$ decreases.



No phase separation for different reps

- ▶ Polyakov loop for F and A_2 at fixed β and κ_4 .
- ▶ All observables respond simultaneously.
- ▶ Same in entire parameter space.
- ▶ **Single transition.**
- ▶ Transition seems first order.

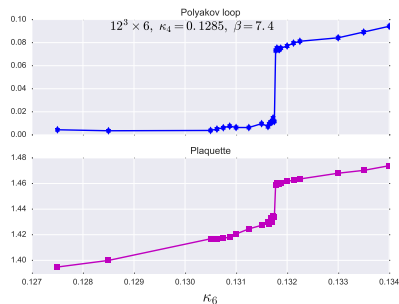
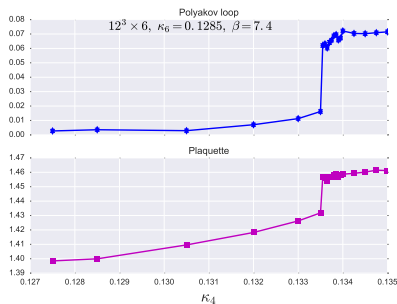


Conclusions

- ▶ Finite temperature study of $SU(4)$ gauge theory with 2 fermion reps.
- ▶ NDS action helps avoid the bulk transition.
- ▶ Confinement transitions for both reps coincide.
- ▶ Chiral transition for both reps? (D. Hackett's talk)

THANK YOU

Order of transition



- Polyakov loop and Plaquette discontinuous \implies 1st order confinement transition.

Higher-rep Polyakov loop

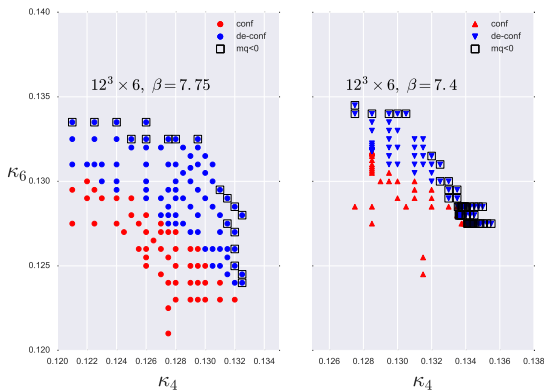
- ▶ $\Omega_x^F = \prod_t U_{x,t}^F$
- ▶ $P^F = \text{Tr} \Omega^F$

- ▶ $\Omega_x^{A_2} = \prod_t U_{x,t}^{A_2}$
- ▶ $P^{A_2} = \text{Tr} \Omega^{A_2}$

- ▶ $U^{A_2} = \frac{1}{2} \left[U_{ij}^F U_{kl}^F - U_{il}^F U_{kj}^F \right]$
- ▶ $P^{A_2} = \frac{1}{2} \left[(\text{Tr} \Omega^F)^2 - \text{Tr} (\Omega^F)^2 \right]$

Comparison for $\beta = 7.75$ and $\beta = 7.4$.

- Curve shifts to the right.



Phase diagram comparison

- ▶ Comparing the confinement transition for F vs A_2 .
- ▶ Both transitions co-incide.

